

# First detection of BAO peak in the three-point correlation function of galaxy clusters

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# Overview

General overview and motivation of 3PCF

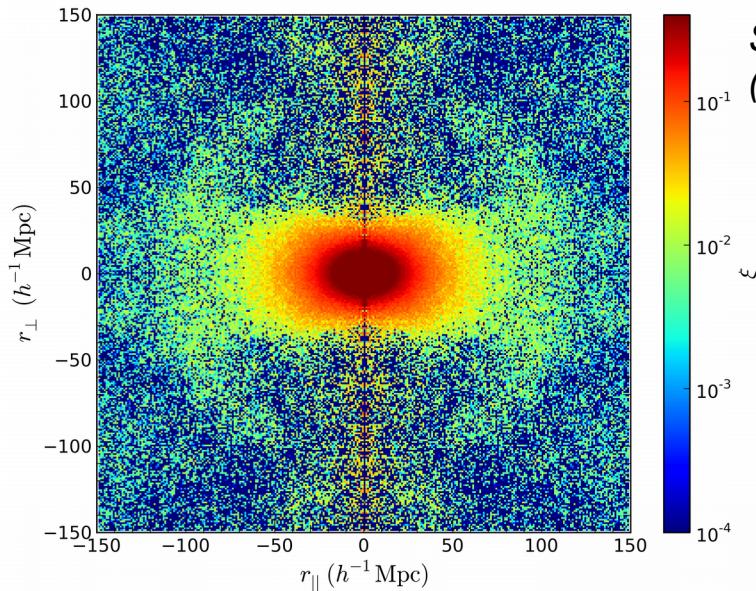
Some applications

Detecting the BAO signal in the 3PCF of galaxy clusters

# Galaxy clustering and cosmology

Galaxy correlation functions encode fundamental information for cosmology

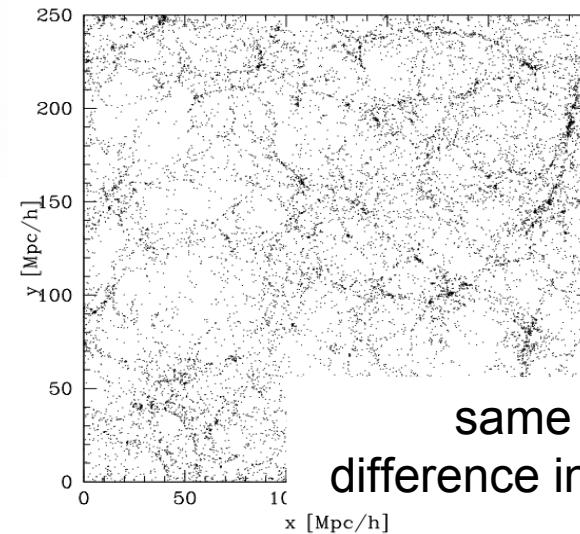
- BAO
- RSD



*Samushia et al.  
(2013)*

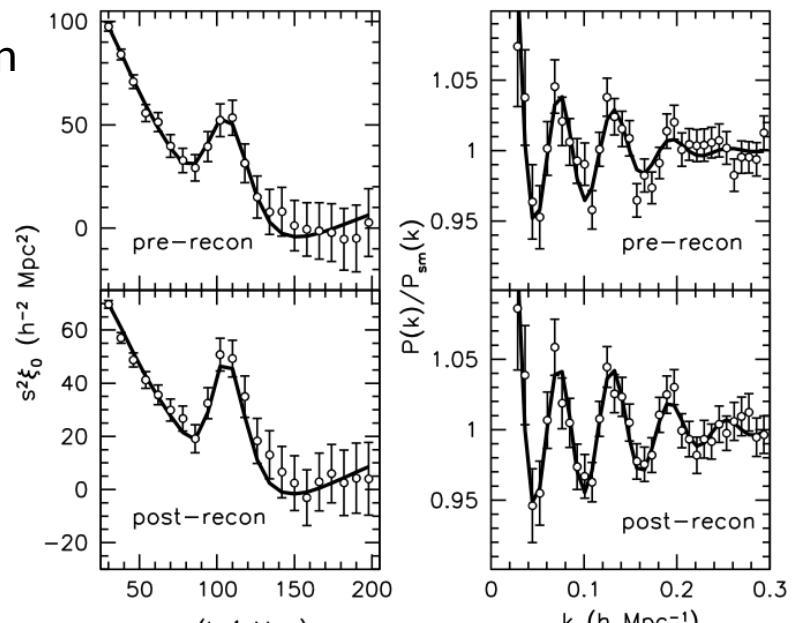
for a Gaussian Random Field,  
2PCF (and/or Pk) would be enough  
(mean and variance)

... but the Universe is just  
not like that!

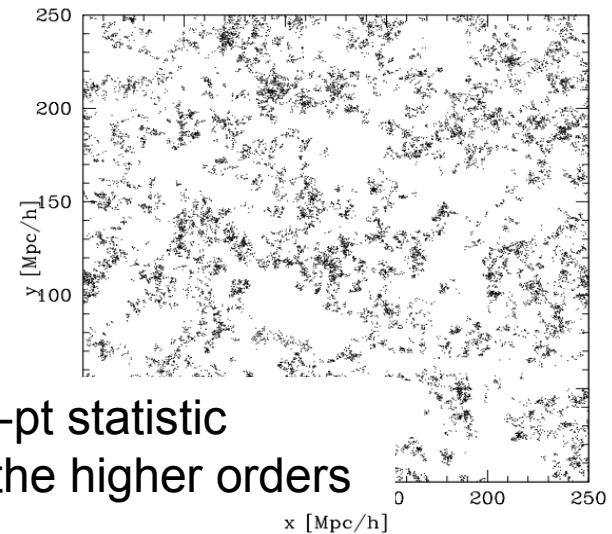


same 2-pt statistic  
difference in the higher orders

*Sefusatti & Scoccimarro (2005)*

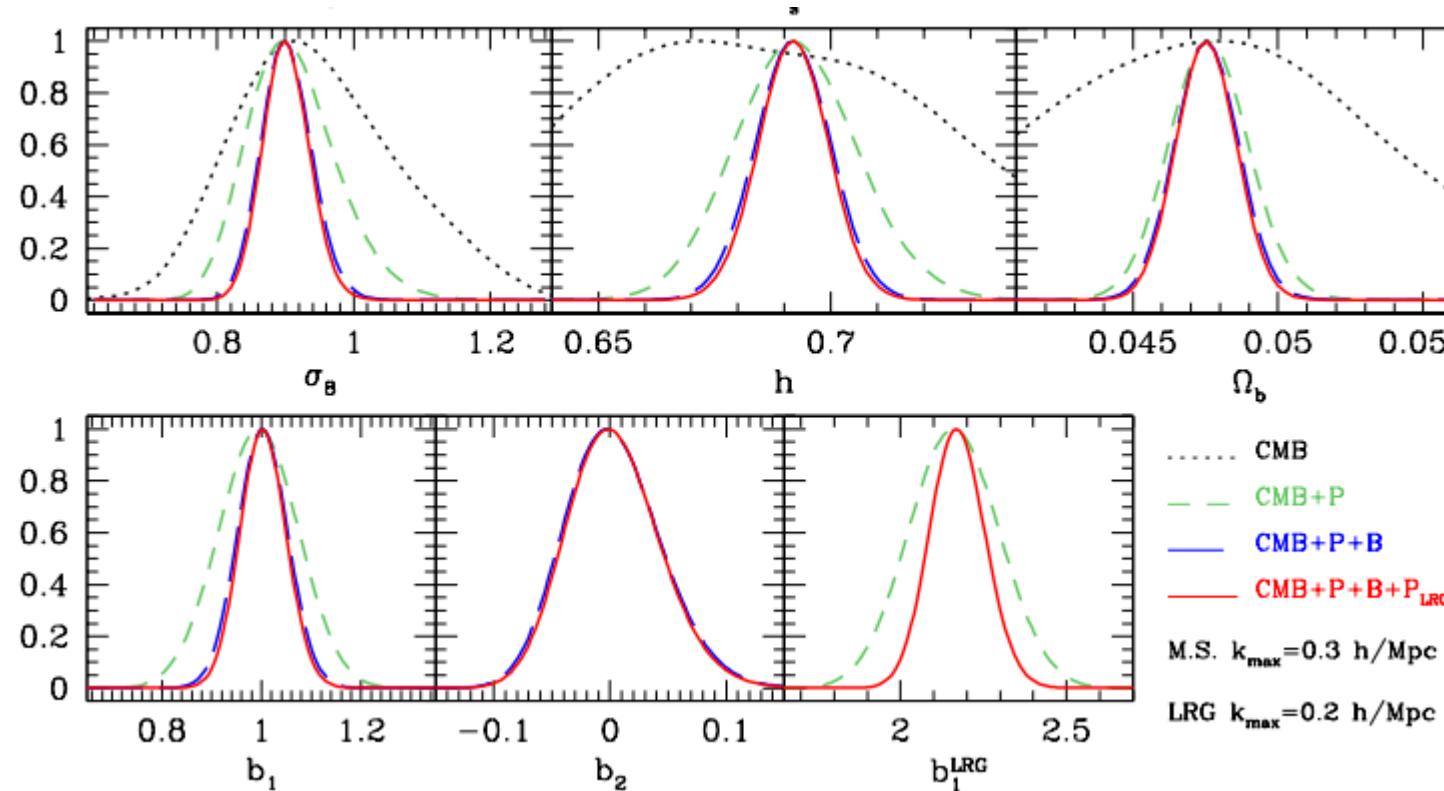
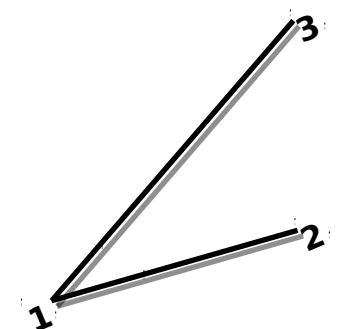


*Anderson et al. (2014)*



# Why moving to higher orders?

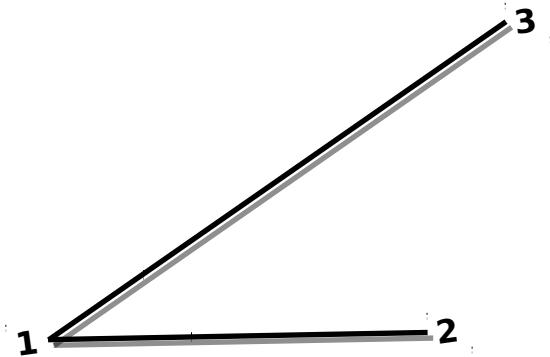
- first significant order to detect non-Gaussian signals
- exploit additional information
- can probe both scale (as the 2PCF) and **shape (unlike the 2PCF)**
- in combination with the 2PCF **can break the degeneracy between bias and  $\sigma_8$**   
=> cosmological constraints
- improve constraints on parameters in combination with CMB and 2PCF



# 3-point functions: a (partial) review

Probability of finding triplets in configurations (3PCF) or Fourier space (bispectrum  $B_k$ )

$$P = [1 + \xi(r_{12}) + \xi(r_{23}) + \xi(r_{31}) + \xi(r_{12}, r_{23}, r_{31})] \times n^3 dV_1 dV_2 dV_3$$



## Bispectrum

- estimators  
*standard, skew, integrated, modal, ... see Regan (2017)*
- measurements on simulations  
*e.g. PTHalos (Sefusatti et al. 2006), DeMNUNI (Ruggeri et al. 2017), DEUS-PUR (Chan&Blot, 2017), but many more...*
- measurements on data  
*CfA Redshift Survey (Baumgart&Fry, 1991), IRAS (Feldman et al., 2001, Scoccimarro et al., 2001), 2dFGRS (Verde el al., 2002), SDSS-LRGs (Gil-Marín et al. 2015a,b), SDSS-BOSS (Gil-Marín et al. 2016), but many more...*
- modelization easier in Fourier space

Much more mature and explored field

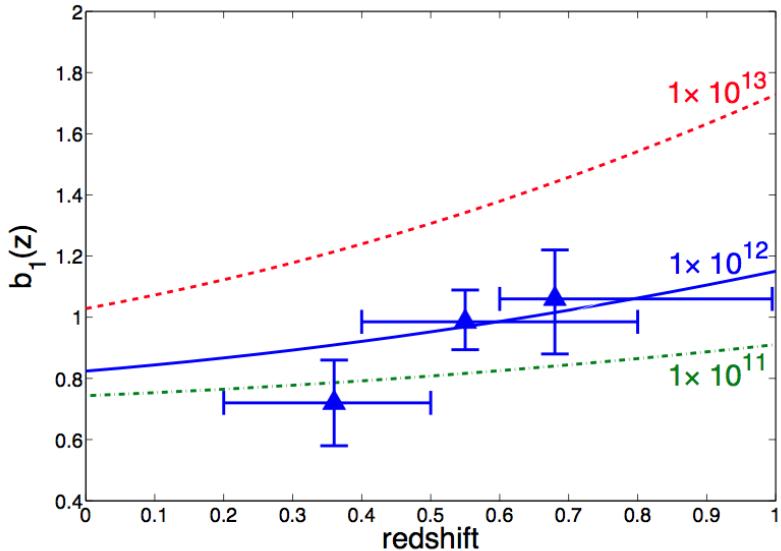
## 3PCF

- estimators  
*Szapudi & Szalay (1998), Slepian & Eisenstein (2015)*
- measurements on simulations  
*CODECS (Moresco et al. 2014), (DeMNUNI), DEUS-PUR (Hoffmann et al. 2018)*
- measurements on data  
*SDSS (Kayo et al., 2004, Nichol et al. 2006, McBride et al., 2011), 2dFGRS (Jing & Börner 2004, Pan & Szapudi 2005), SDSS-LRGs (Marin et al. 2011), SDSS-BOSS (Slepian et al. 2017), Wigglez (Marin et al. 2013), VIPERS (Moresco et al. 2016)*
- modelization more difficult  
*mixing of small- and large-scales modes*

Many aspects still to be explored!

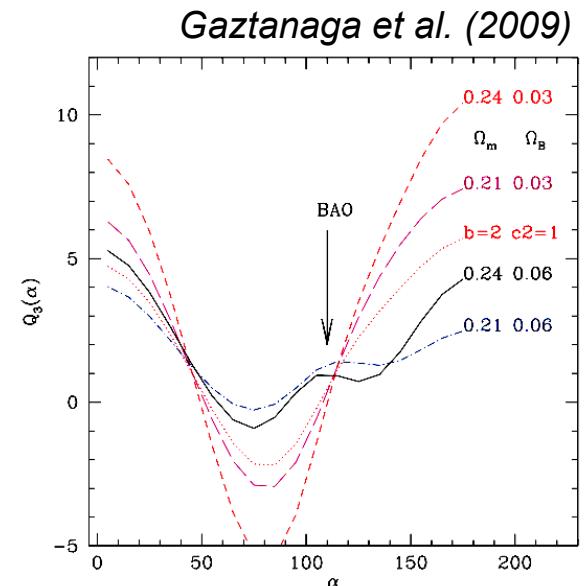
# Status of the art

- dependence on **color, luminosity and stellar mass**  
e.g. Jing & Borner 2004, Kayo et al. 2004, McBride et al. 2011,  
Guo et al. 2014, Moresco et al. (2016)
- cosmology-independent measure of **galaxy bias**  
e.g. McBride et al. (2011), Marin et al. (2011), Marin et al. (2013)
- study **different estimators**  
e.g. Slepian & Eisenstein (2015a,b)
- disentangle **different cosmologies and neutrino masses**  
e.g. Moresco et al. (2014)
- **BAO detection**  
e.g. Gaztanaga et al. (2009), Slepian et al. (2016)

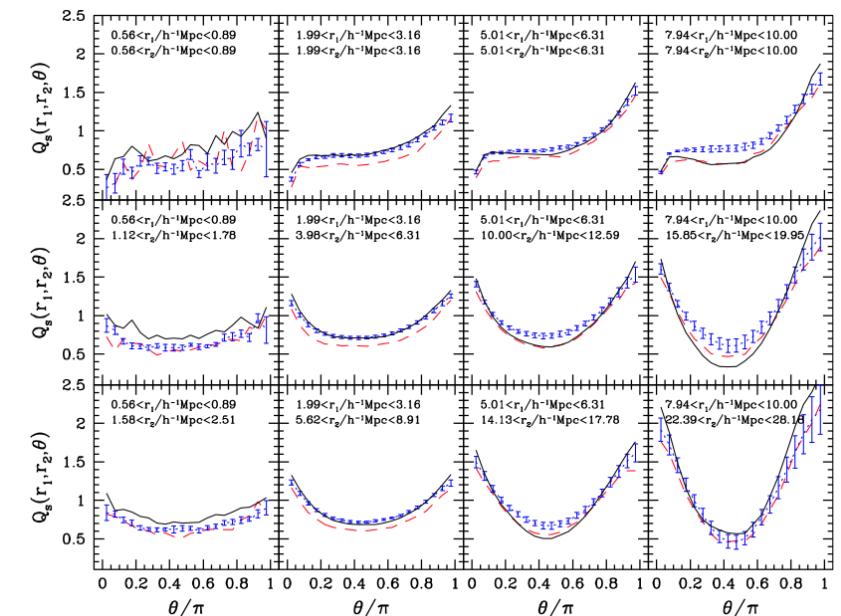


Marin et al.  
(2013)

significant work on  
galaxy evolution



Guztanza et al. (2009)



Guo et al. (2014)

# Definition and estimators

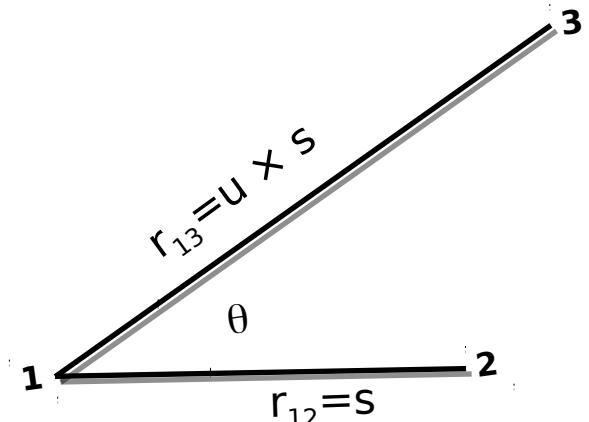
3PCF estimator

Szapudi & Szalay (1998)

data catalog

$$\xi = \frac{DDD - 3DDR + 3DRR - RRR}{RRR}$$

random catalog



$$r_{12} = s$$

$$r_{13} = u \times s$$

$$r_{23} = s \times (1 + u^2 - 2 \times u \times \cos \theta)^{1/2}$$

$$\text{binning } \Delta r_{ij}/r_{ij} = \text{cost}$$

Marin et al. (2011)

2PCF estimator

Landy & Szalay (1993)

$$\xi = \frac{DD - 2DR + RR}{RR}$$

connected 3PCF

$$\xi(r_{12}, r_{13}, \theta)$$

$$\propto b^3 \sigma_8^4$$

reduced 3PCF

$$Q(r_{12}, r_{13}, \theta) = \frac{\xi(r_{12}, r_{13}, \theta)}{\xi(r_{12})\xi(r_{23}) + \xi(r_{23})\xi(r_{31}) + \xi(r_{31})\xi(r_{12})}$$

$$\propto b^{-1}$$

# The code: CosmoBolognaLib



## CosmoBolognaLib

Open Source C++ libraries for cosmological calculations

Main Page

Modules

Namespaces

Classes

Files

Examples

Search

▼ CosmoBolognaLib



The CosmoBolognaLib documentation

► Modules

► Namespaces

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► Files

► Examples

### The CosmoBolognaLib documentation

Here you can find the full documentation of the **CosmoBolognaLib**, a large set of Open Source C++ libraries for cosmological calculations. Among many other things, these libraries can be used to measure the two-point and three-point correlation functions, and to model redshift-space distortions and baryon acoustic oscillations.

Please have a look at the example codes in `CosmoBolognaLib/Examples/` that show how to use the CosmoBolognaLib in either **C++** or **Python** codes.

## C++ and python libraries for cosmological calculation

**Code.** <https://github.com/federicomarulli/CosmoBolognaLib>

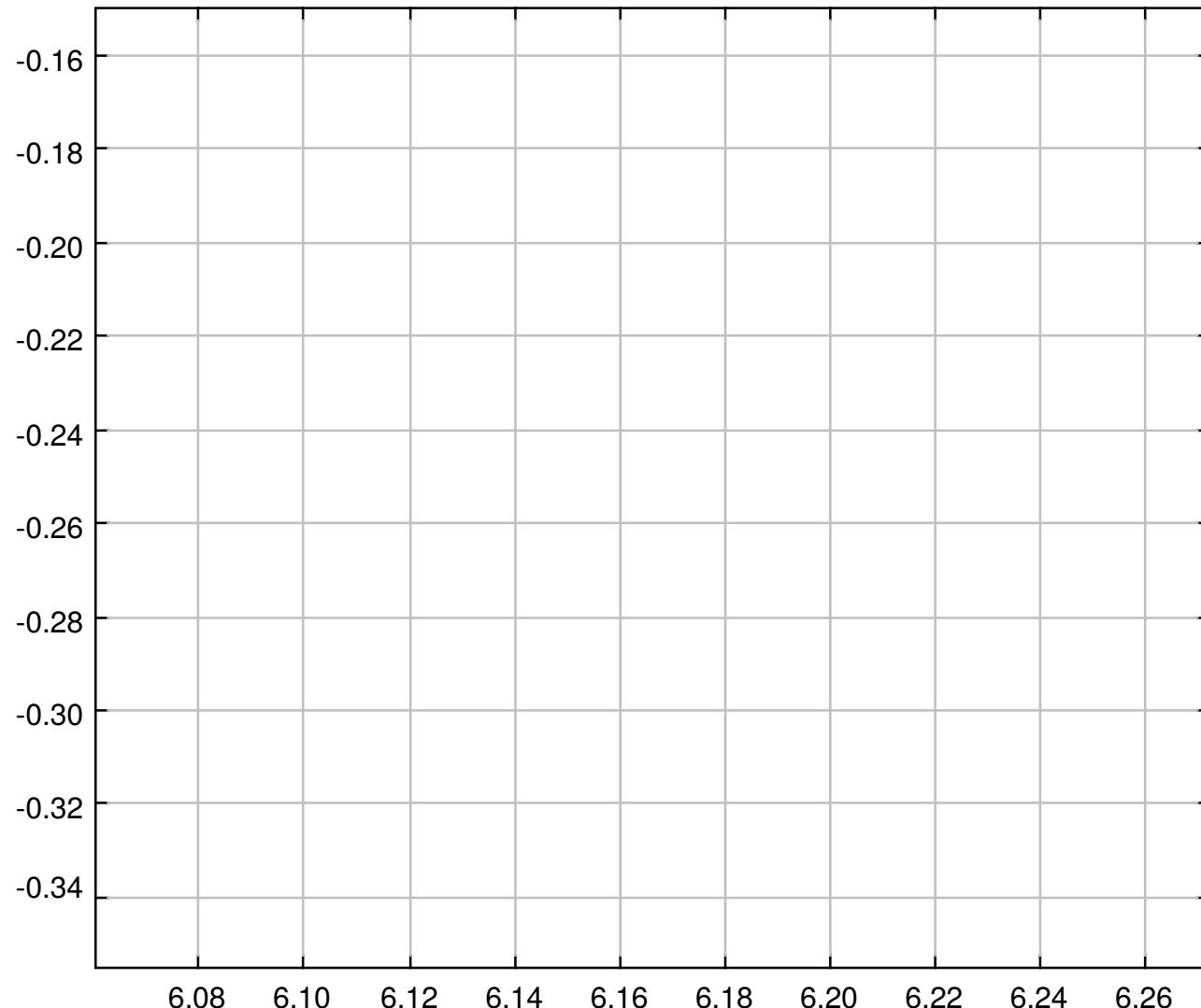
**Doc.** <http://apps.difa.unibo.it/files/people/federico.marulli3/CosmoBolognaLib/Doc/html/index.html>

**Ref.** Marulli, Veropalumbo & Moresco (2016, arXiv:1511.00012)

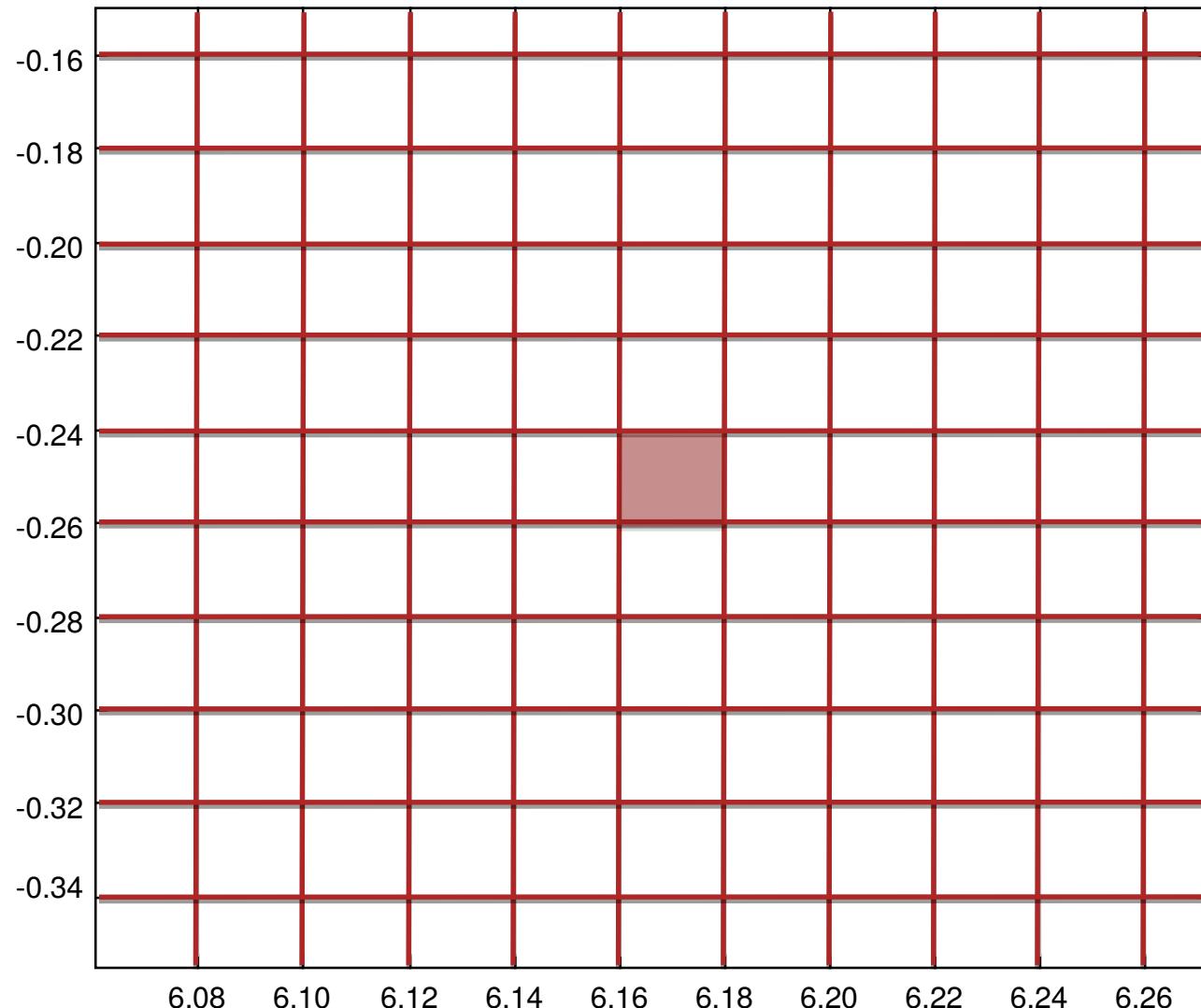
Extensive 2PCF measurements and modelling. For the 3PCF:

- measure the connected  $\zeta$  and reduced 3PCF Q in different configurations
- implement a double chain-mesh technique
- binning as a function of  $\theta$  or  $r$
- errors with integrated JK and/or BS
- modelization of both  $\zeta$  and Q
- MCMC adopting the stretch move ensemble sampler (Goodman & Weare, 2010)

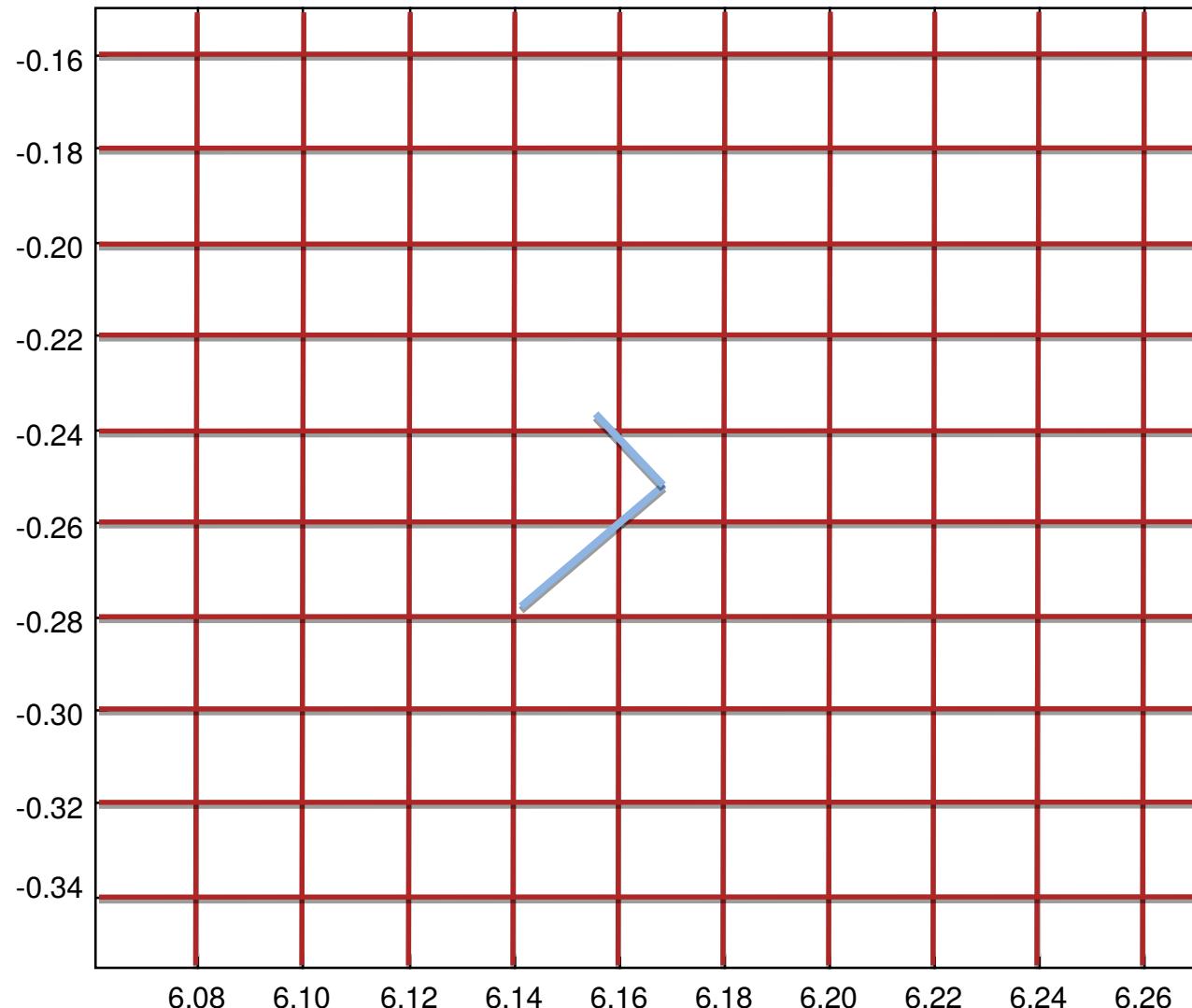
# Chain-mesh approach



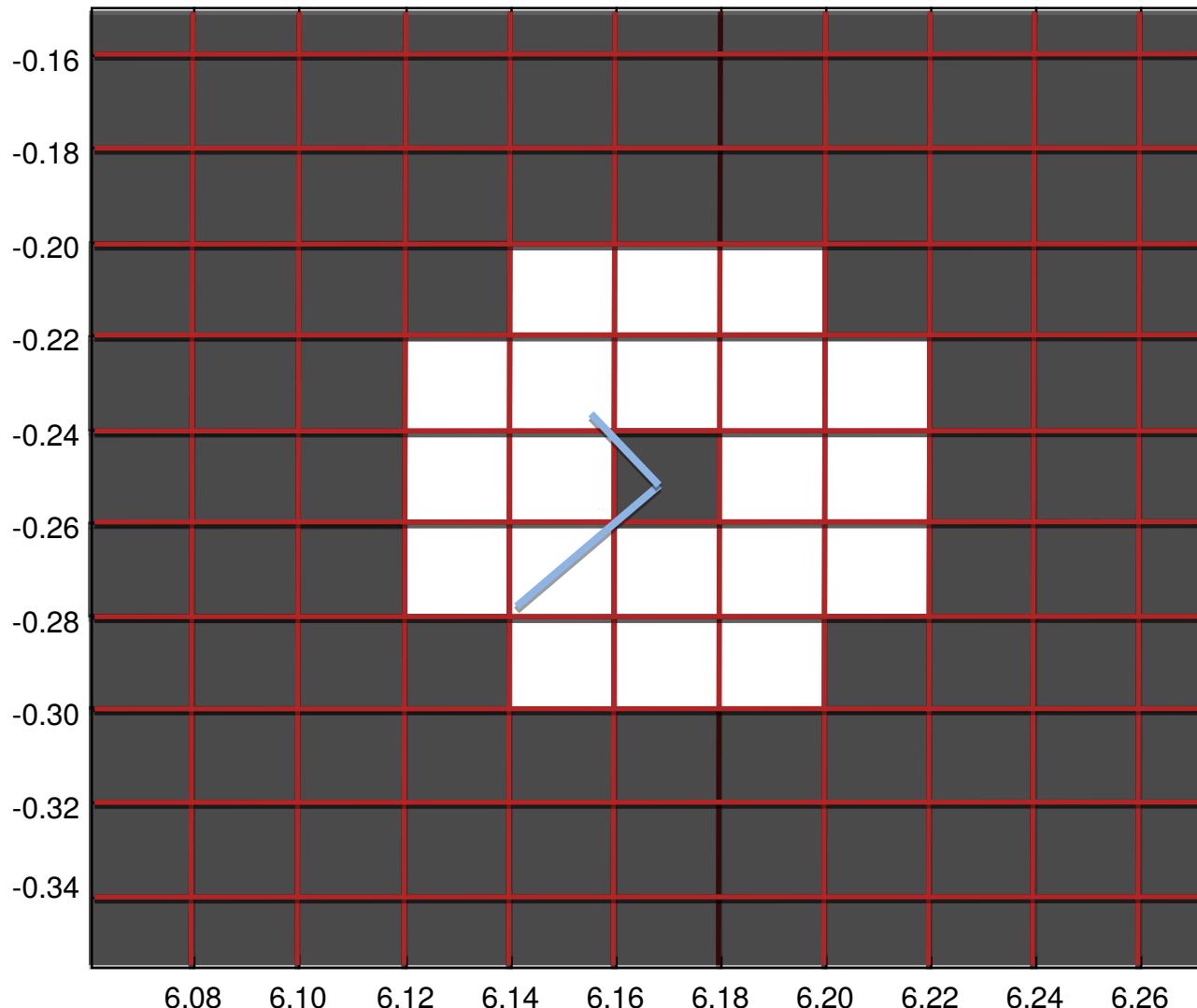
# Chain-mesh approach



# Chain-mesh approach



# Chain-mesh approach



# Some application of the 3PCF

# Exploring 3PCF in simulations

## CODECS simulations

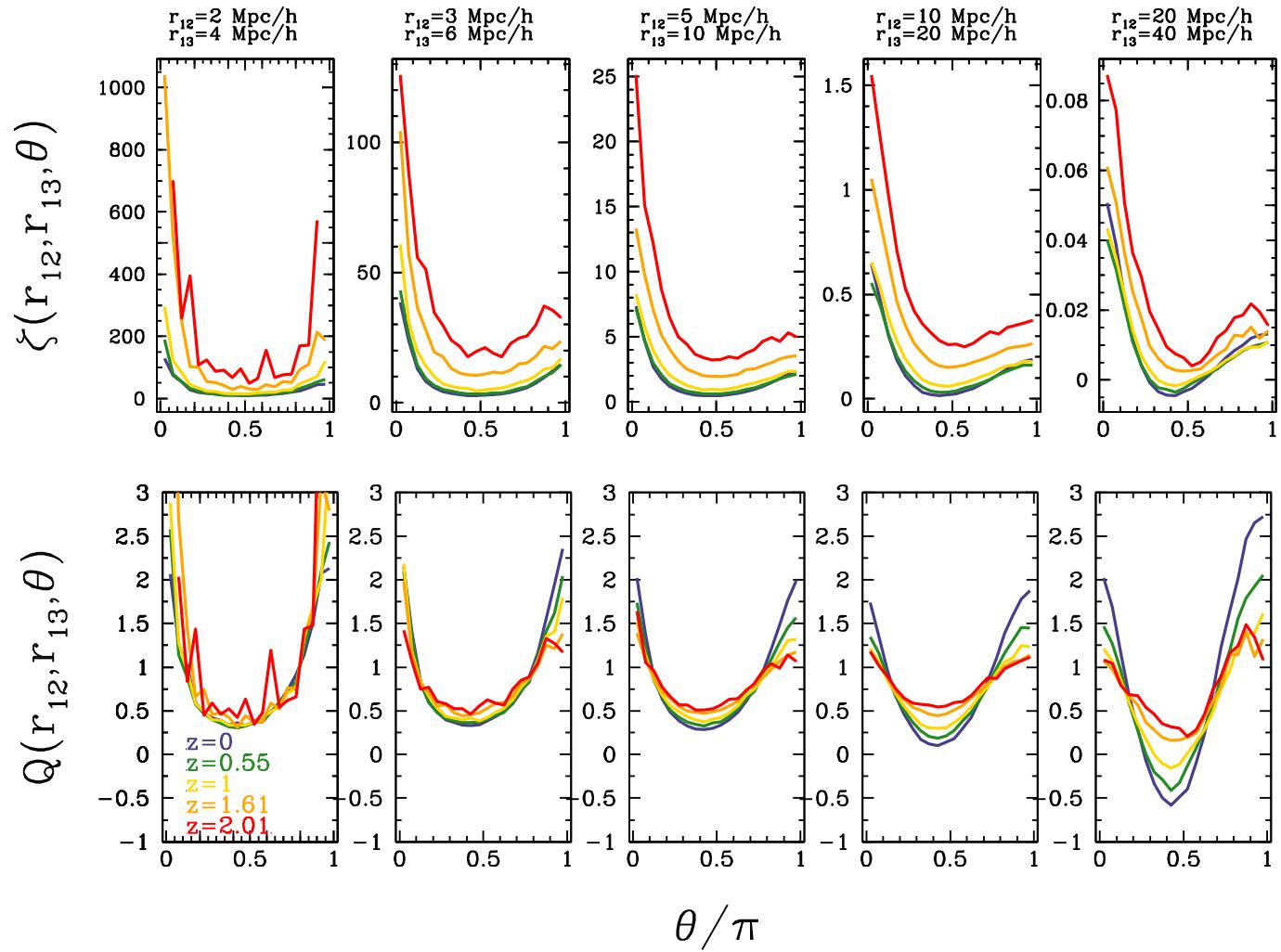
Baldi (2012)

5 cDE models + LCDM(WMAP7yr),  
 $N_p=2 \times 1024^3$ ,  $L_{\text{box}}=1 \text{ Gpc}/h$ ,  
 $M_p=5.84 \times 10^{10} M_{\text{sun}}/h$

interacting dark energy  
cosmologies + LCDM

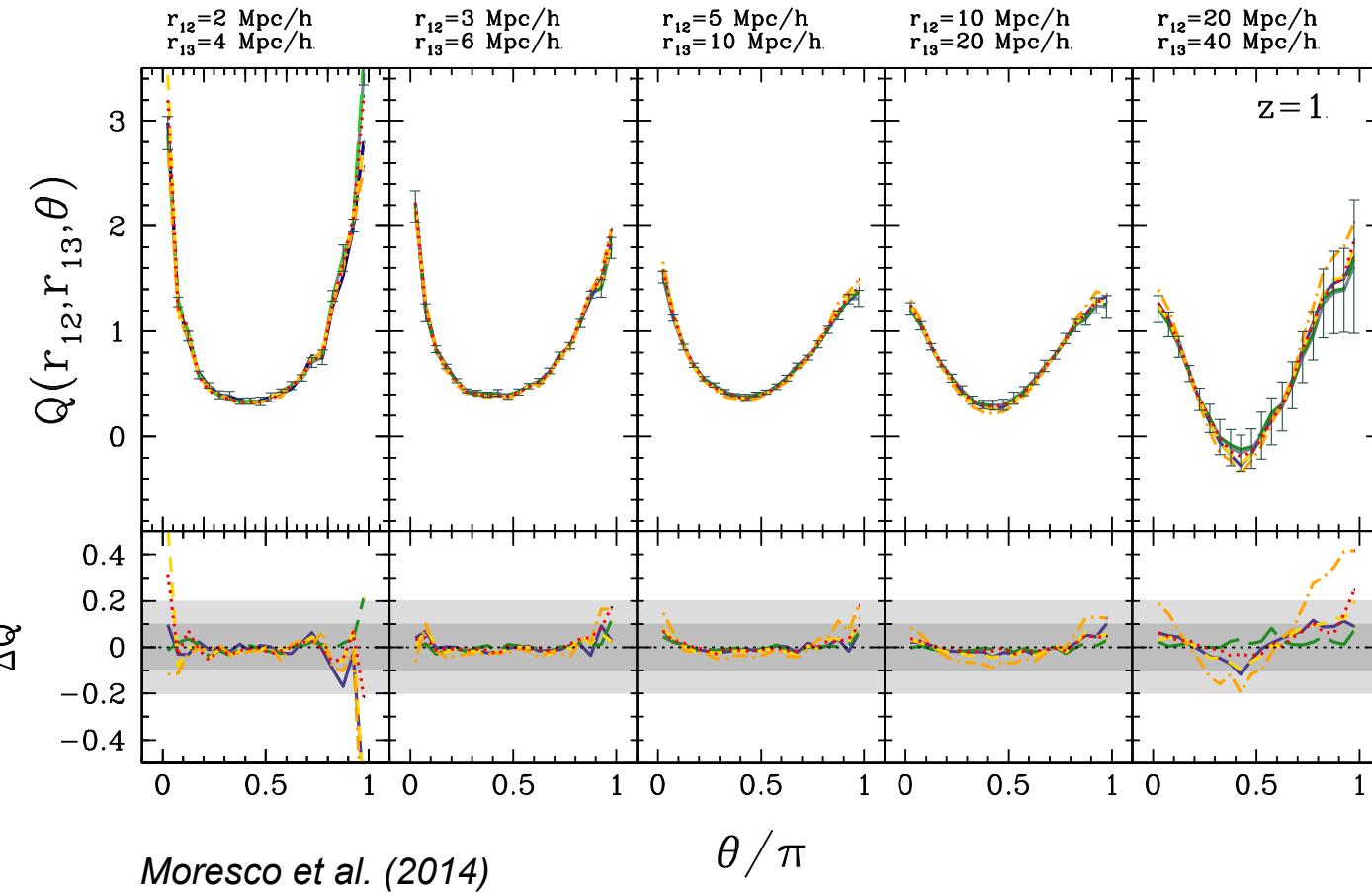
5 different redshifts analyzed  
5 scales

- confirm the transition from the U-shape to V-shape
- witnessing the build-up filaments with redshift

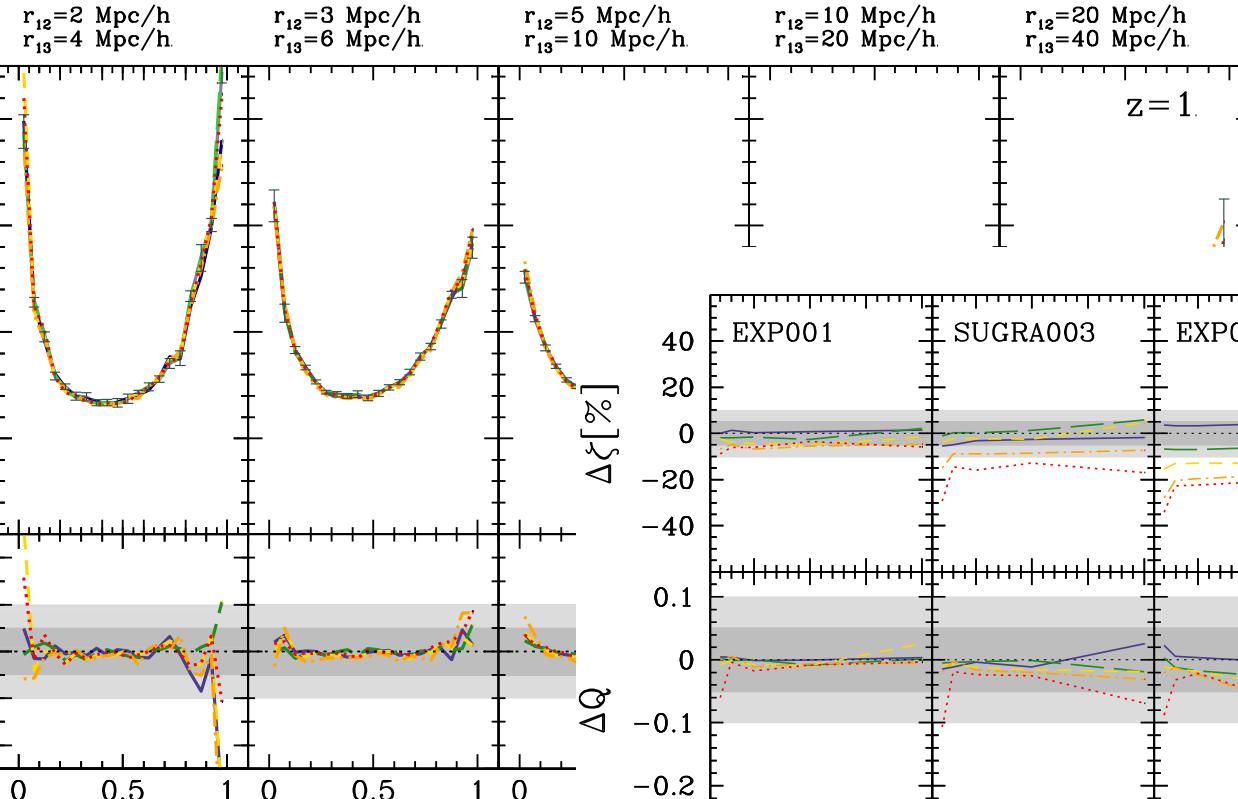


Moresco et al. (2014)

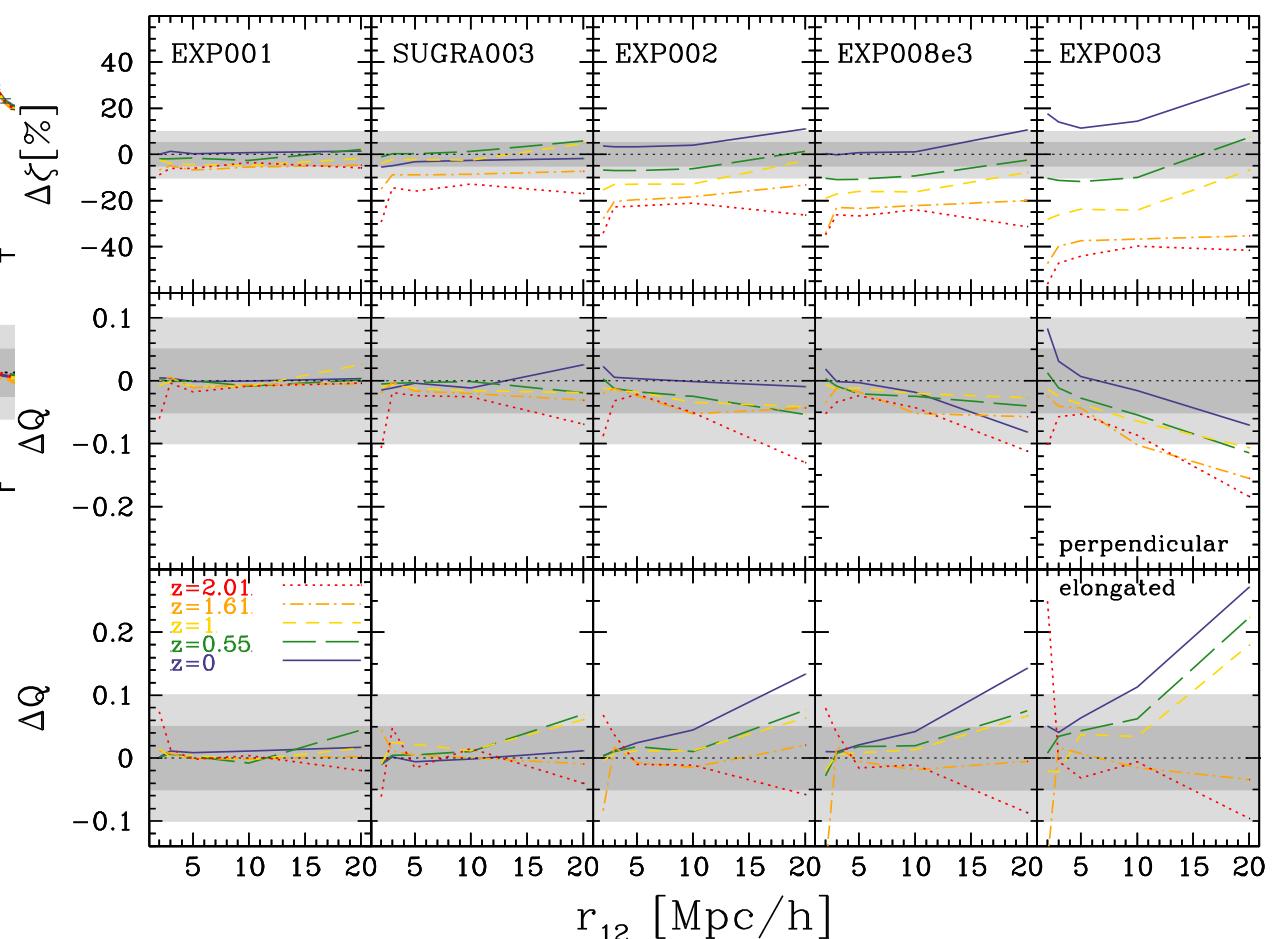
# Disentangling $\Lambda$ CDM with 3PCF



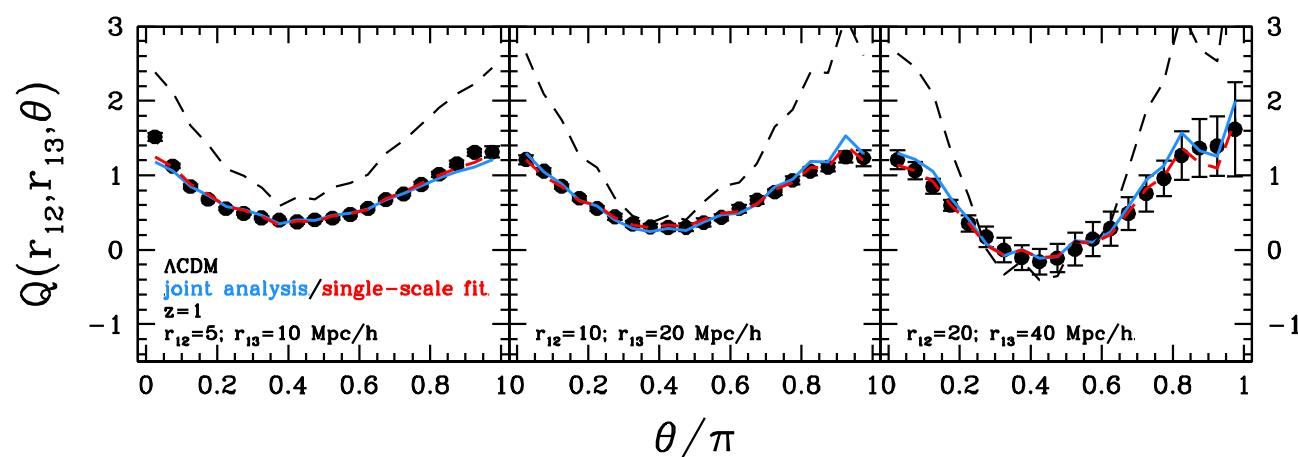
# Disentangling $\Lambda$ CDM with 3PCF



Moresco et al. (2014)



# To the halo bias



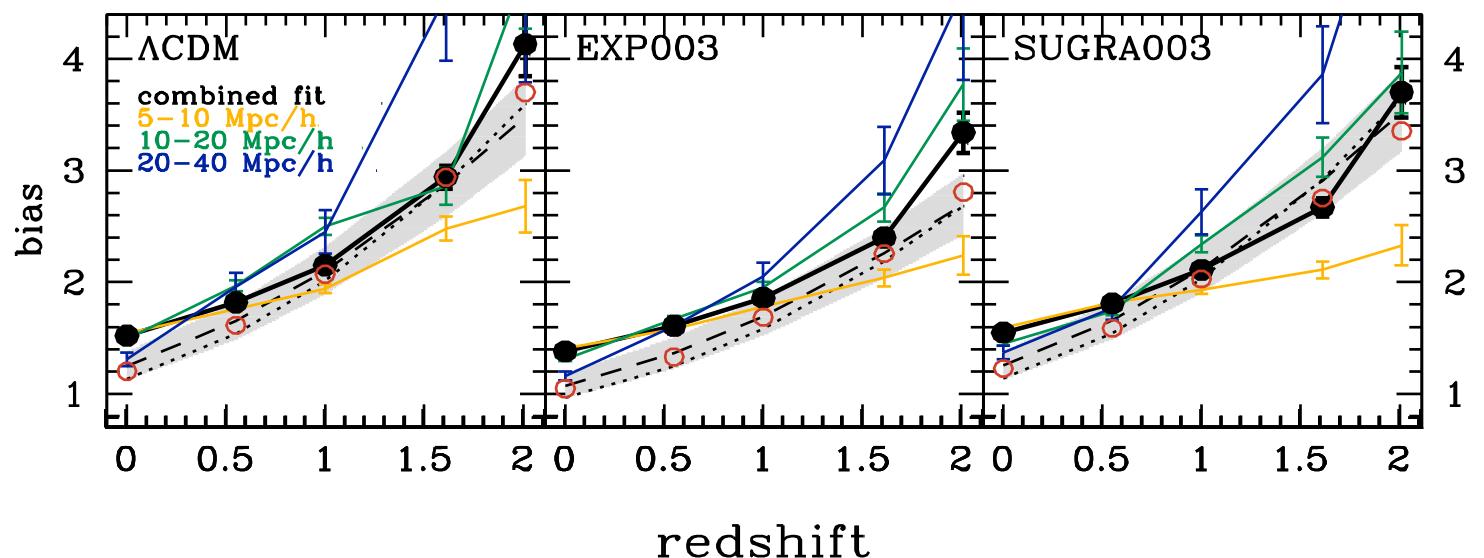
$$Q_h = \frac{1}{b_1} \left( Q_{dm} + \frac{b_2}{b_1} \right)$$

local bias model

- possibility to use 3PCF to **discriminate** between standard and non-standard cosmologies
- **cosmology-independent** bias

**N.B.**

- To be included non-local bias term e.g. see Bel et al. (2015)



# A sneak peak on neutrino masses

## DEMNUNI simulations

Carbone et al. (2016)

3 neutrino masses + LCDM (Planck13)

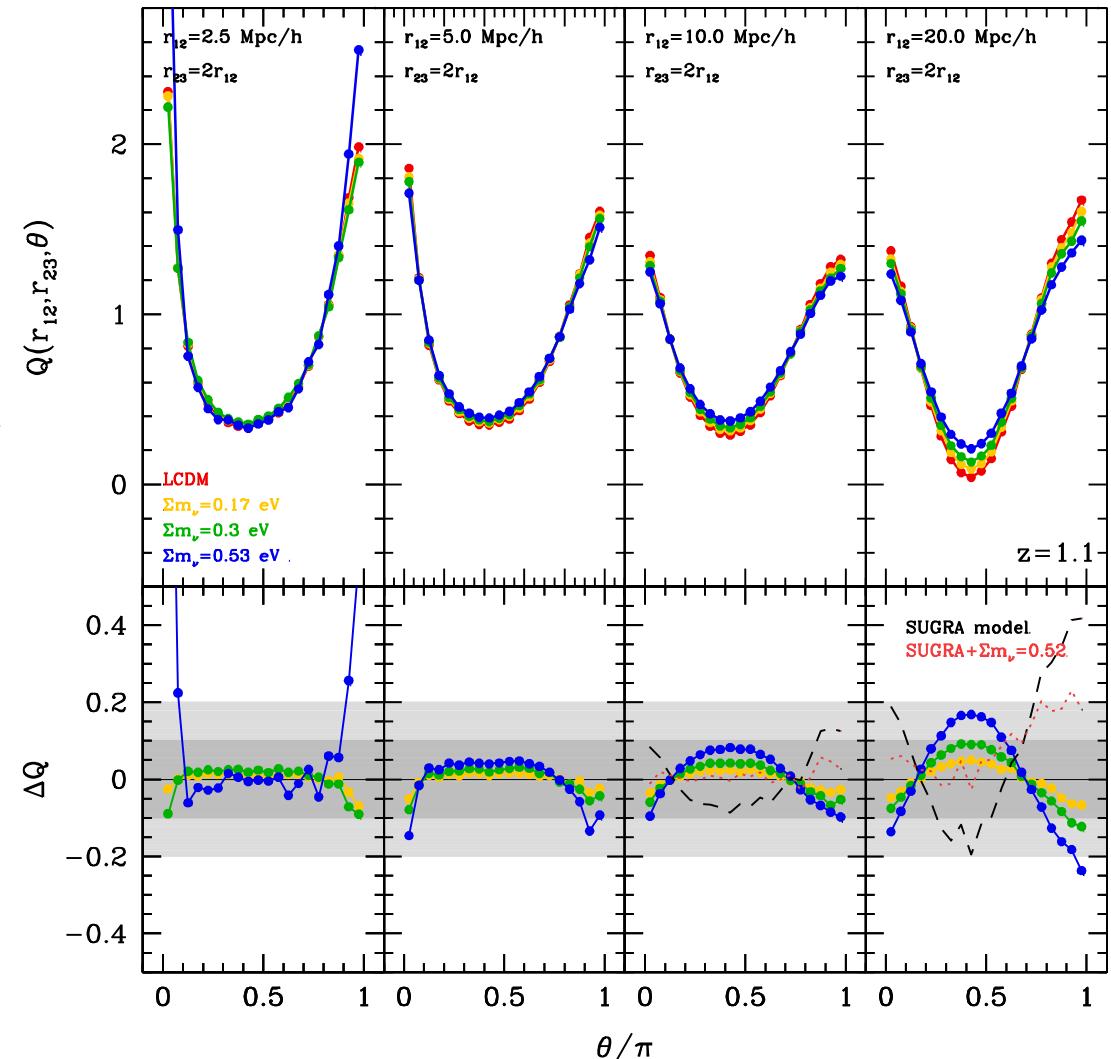
$N_p = 2 \times 2048^3$  (nu included),  $L_{\text{box}} = 2 \text{ Gpc}/h$

$M_p = 8.27 \times 10^{10} M_{\text{sun}}/h$ , 62 snaps with  $z_{\text{in}} = 99$

the largest cosmological simulation with massive neutrinos, suited for both galaxy clustering and lensing Euclid analysis

5 redshifts analyzed, 4 scales

- first 3PCF with massive neutrino cosmologies
- using higher-order correlation functions to constrain neutrino masses

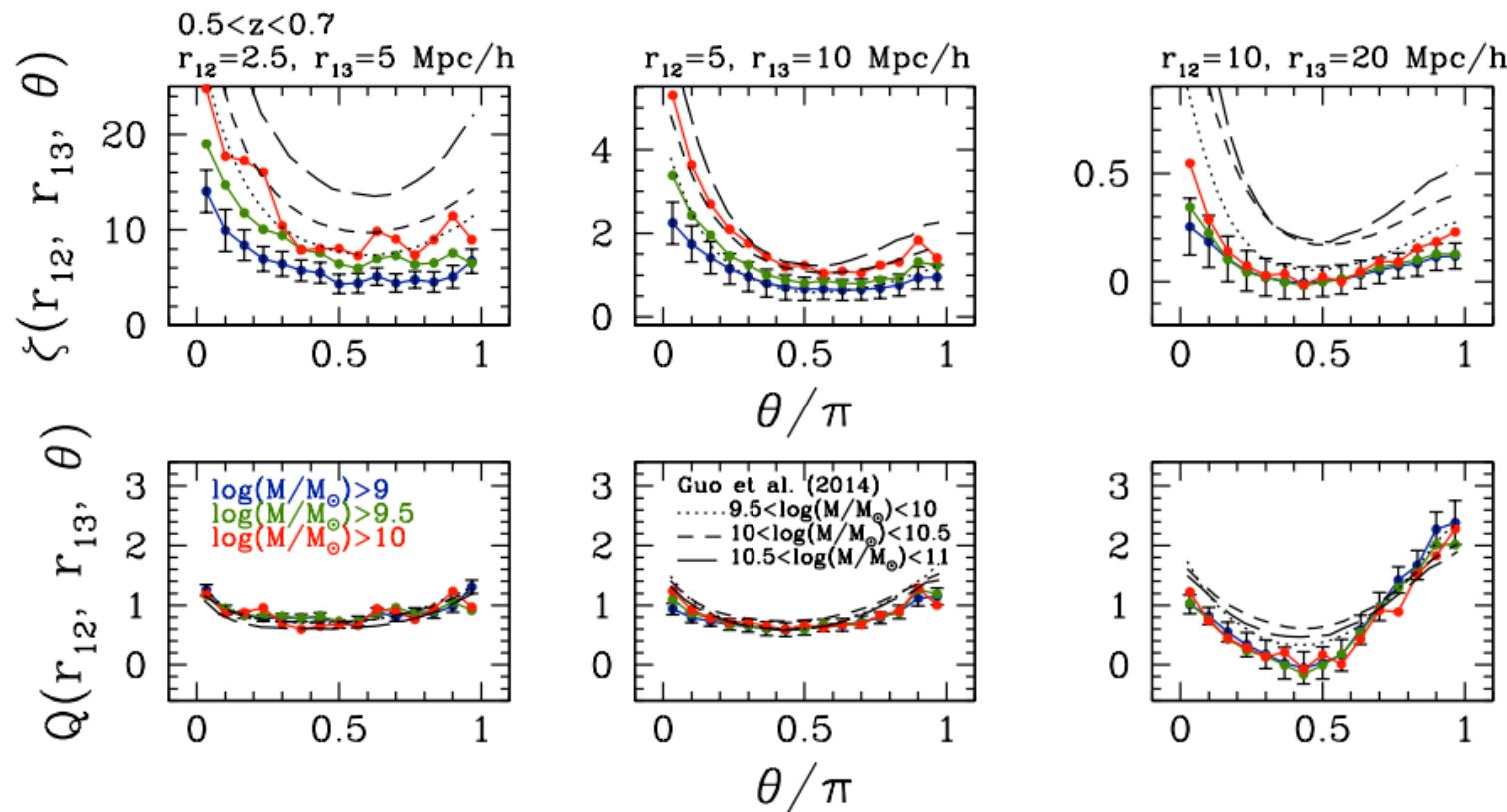
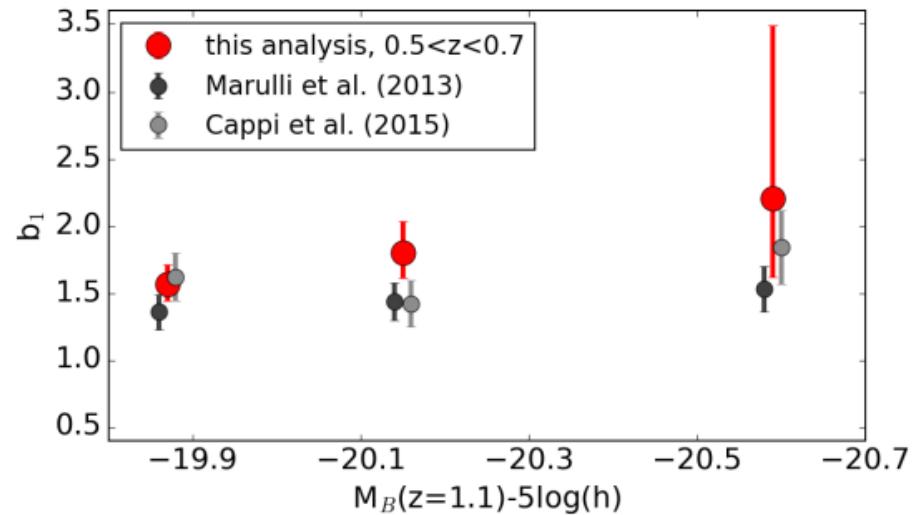


# 3PCF measurements in VIPERS

## VIPERS survey

Guzzo et al. (2014)

spectroscopic survey of  $\sim 100000$  galaxies at  $0.5 < z < 1.1$ , 3 redshift bins, 5 magnitude bins and 4 stellar mass bins, 3 scales ( $r_{12}=2.5, 5, 10$  Mpc/h)



Moresco et al. (2017)

# BAO signal detection in the 3PCF of galaxy clusters

# The BOSS cluster catalog

Original catalog from Wen et al. (2012)

132683 clusters from SDSS-DR8 photo. identified with FoF

$$N_{200} > 8, M_{200} > 0.6 \times 10^{14} M_{\text{sun}}$$

Cross-correlated with spec. info from SDSS-MGS,  
BOSS-LOWZ and BOSS-CMASS

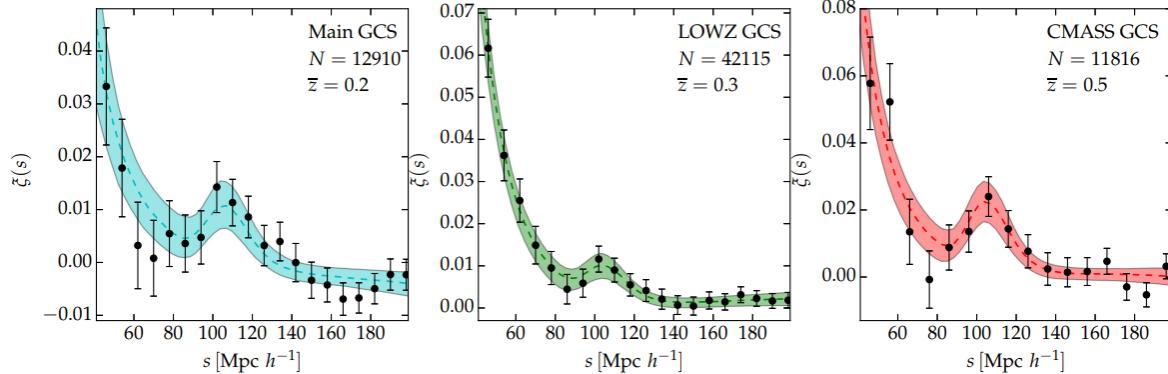
72563 clusters spec. identified (BCG)

$$\langle z \rangle = 0.38$$

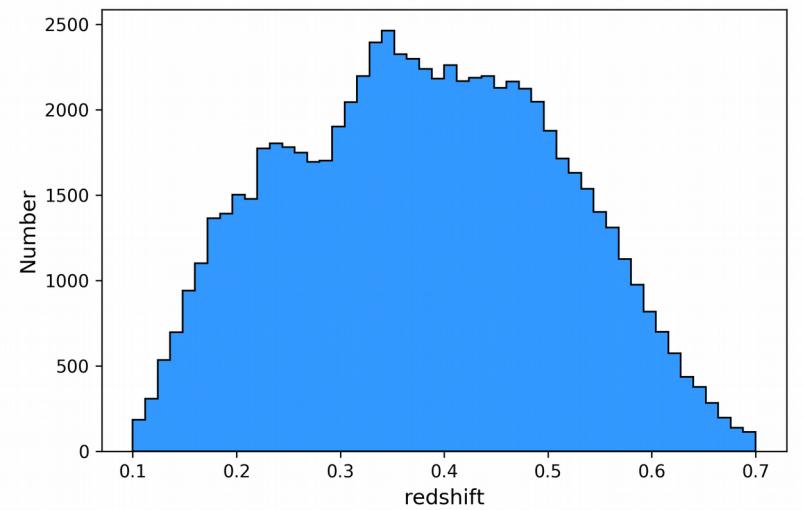
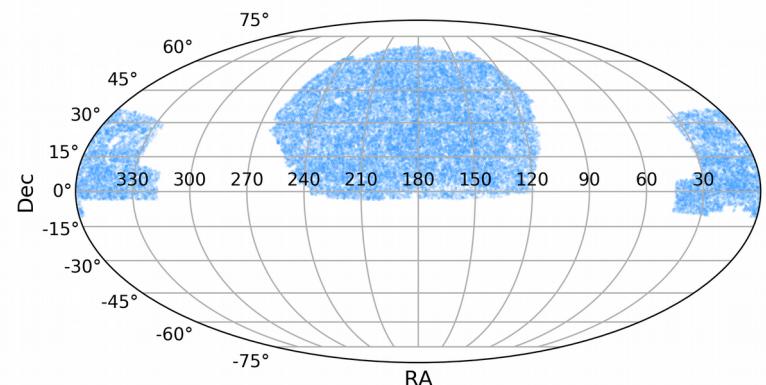
Smaller impact of non-linear distortions

Neat detection of BAO peak in 2PCF

(Veropalumbo et al. 2016)



Veropalumbo et al. (2016)



Moresco et al. (in prep)

# Constraining the bias parameter

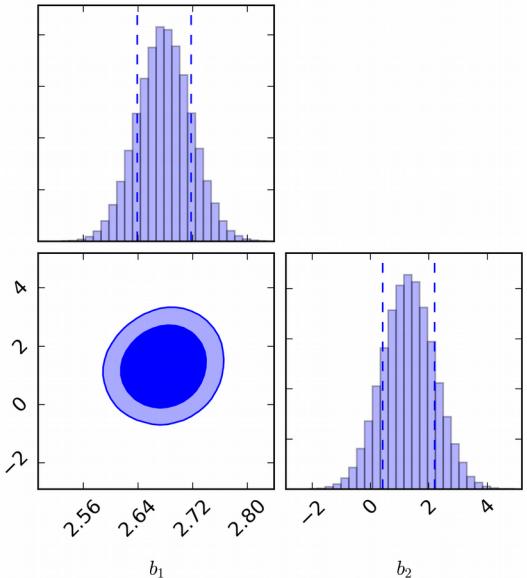
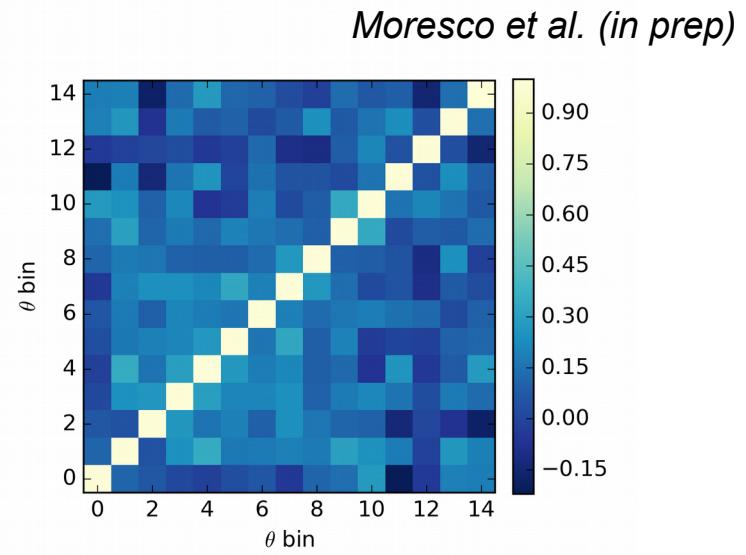
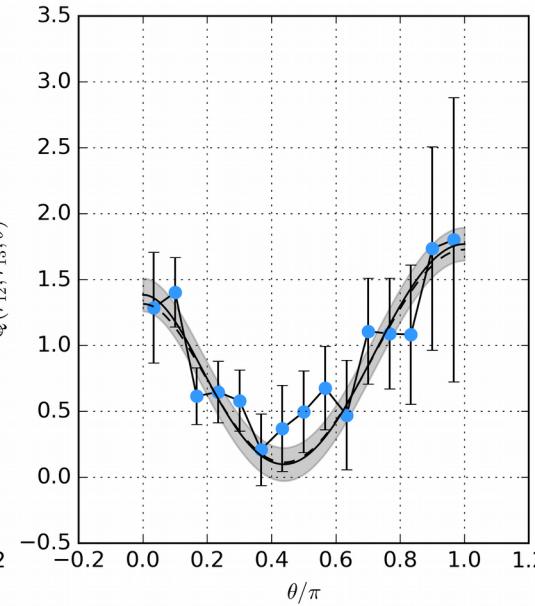
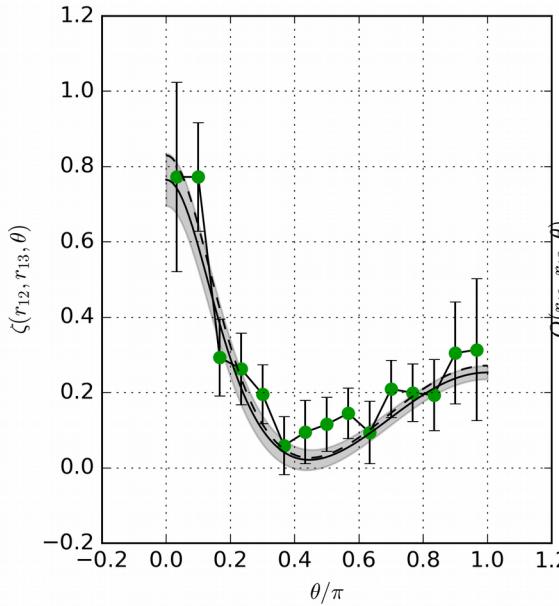
- Measured connected and reduced 3PCF at different scales
- covariance matrix estimated with JK
- fit on Q (independent on  $\sigma_8$ )
- assumed a Gaussian prior on  $b_1$  from 2PCF ( $b_1 = 2.67 \pm 0.04$ )

- local bias model: 1 free parameter ( $b_2$ )
- also test with non-local bias model

$$Q_g = \frac{1}{b_1} \left( Q_m + \frac{b_2}{b_1} + g_2 Q_{nl} \right)$$

*Bel et al. (2015)*

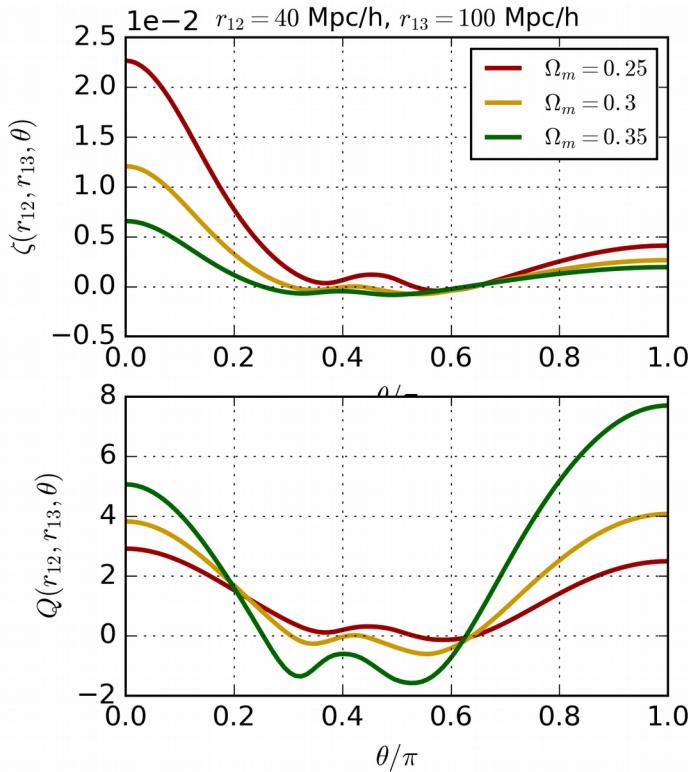
→  $r_{13}$  probing scales [20-50] and [50-80] Mpc/h  
 $b_2 = 1.4 \pm 0.7$



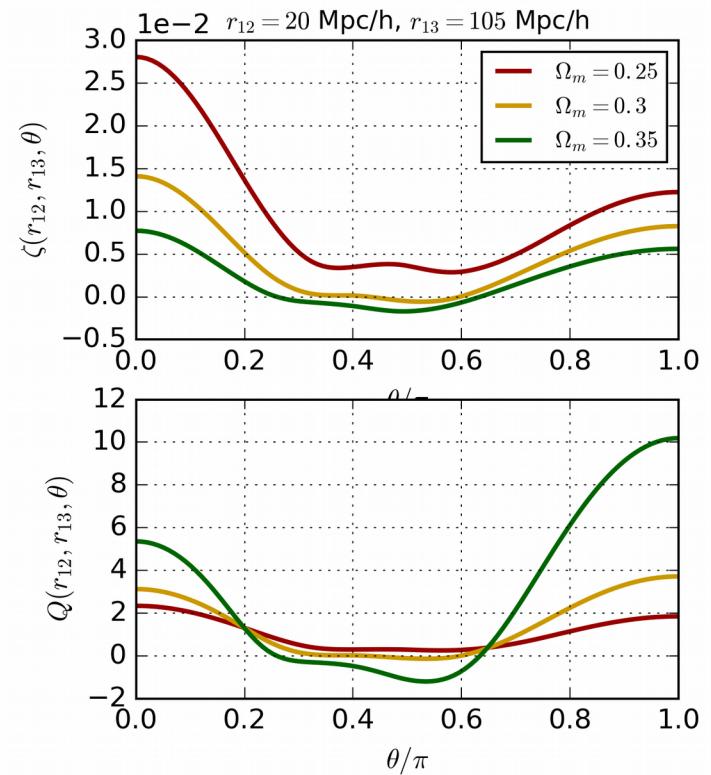
# Detection of BAO peak 1/3

The BAO peak appear summed with the expected dip in the shape dependence of the 3PCF

- smaller range of  $r_{23}$  ==> higher SNR ==> more dispersed signal (only a flattening)  
larger range of  $r_{23}$  ==> lower SNR ==> more concentrated signal (but larger errors)



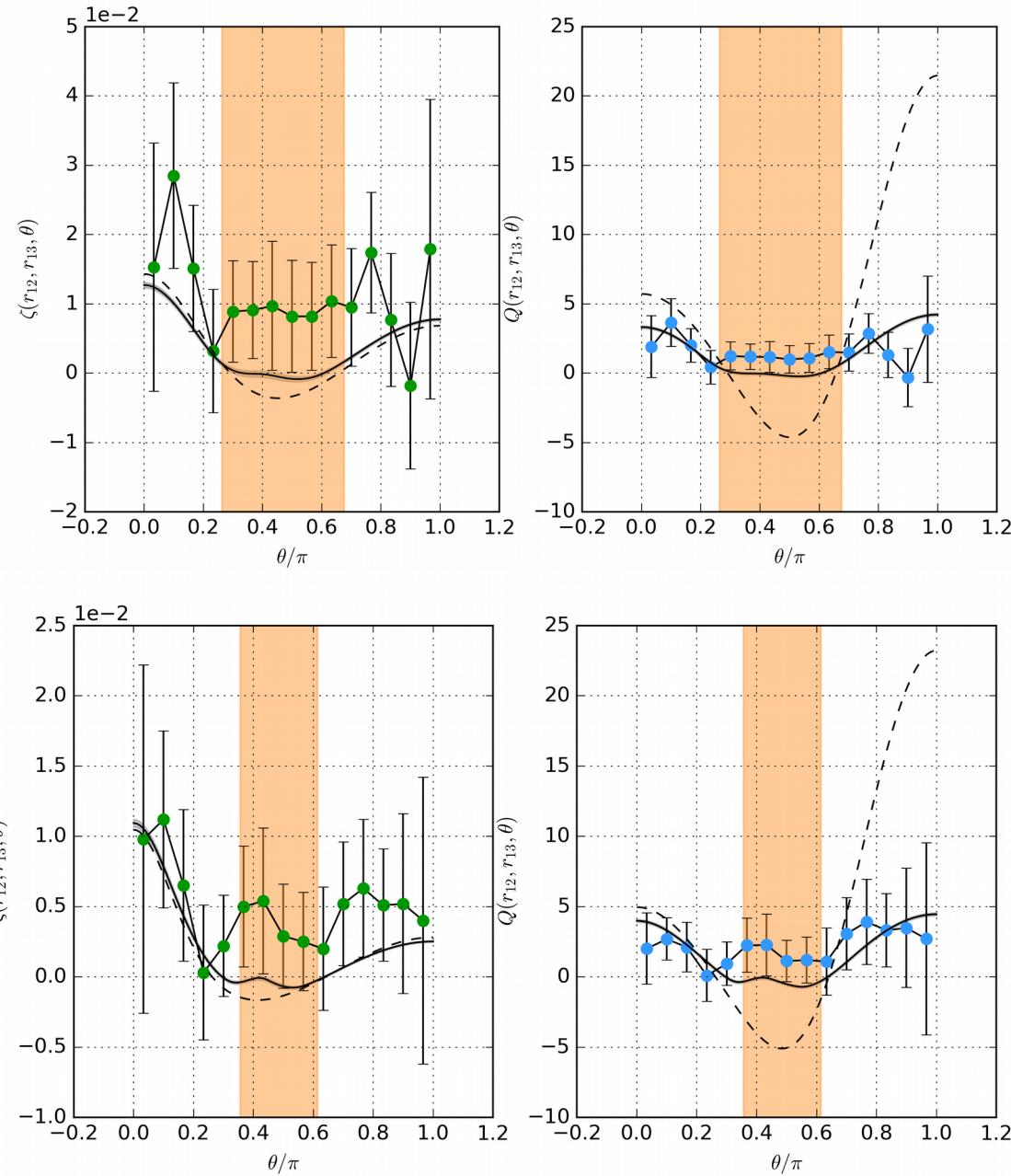
Different configurations explored for both cases,  
Q appears more sensitive



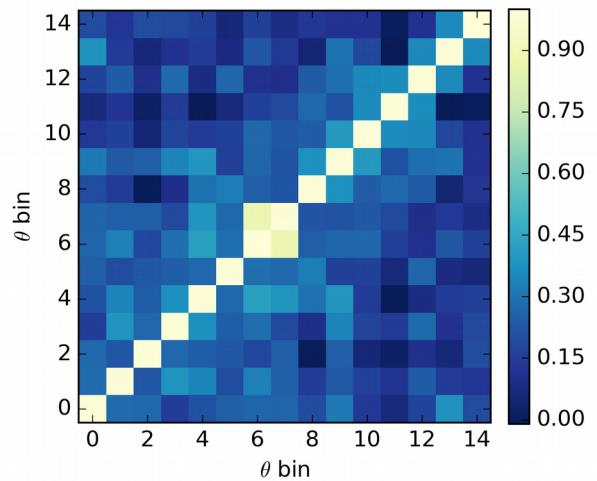
Moresco et al. (in prep)

# Detection of BAO peak 2/3

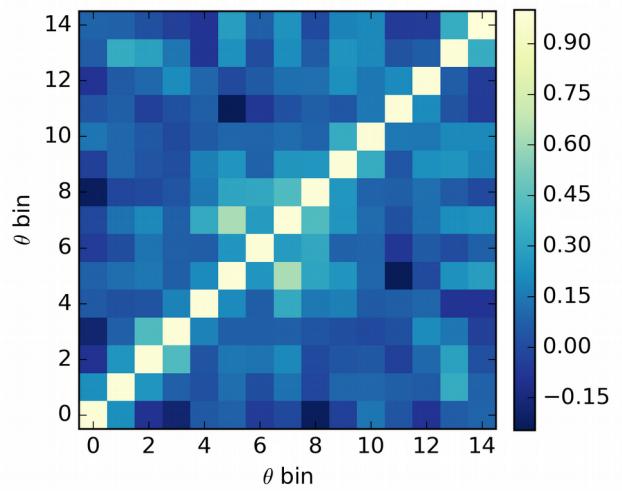
squeezing the BAO signal



$$r_{12} = 25, r_{23} = 105, r_{13} = [80-130] \text{ Mpc/h}$$



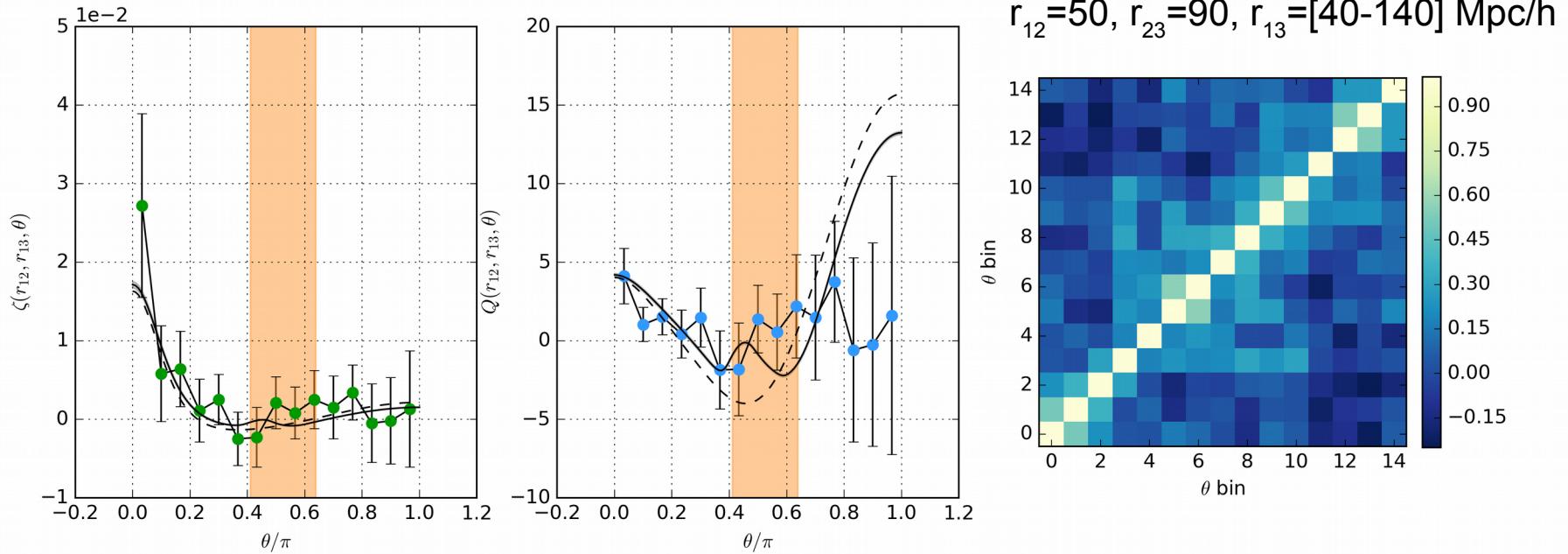
$$r_{12} = 40, r_{23} = 100, r_{13} = [60-140] \text{ Mpc/h}$$



Moresco et al. (in prep)

# Detection of BAO peak 3/3

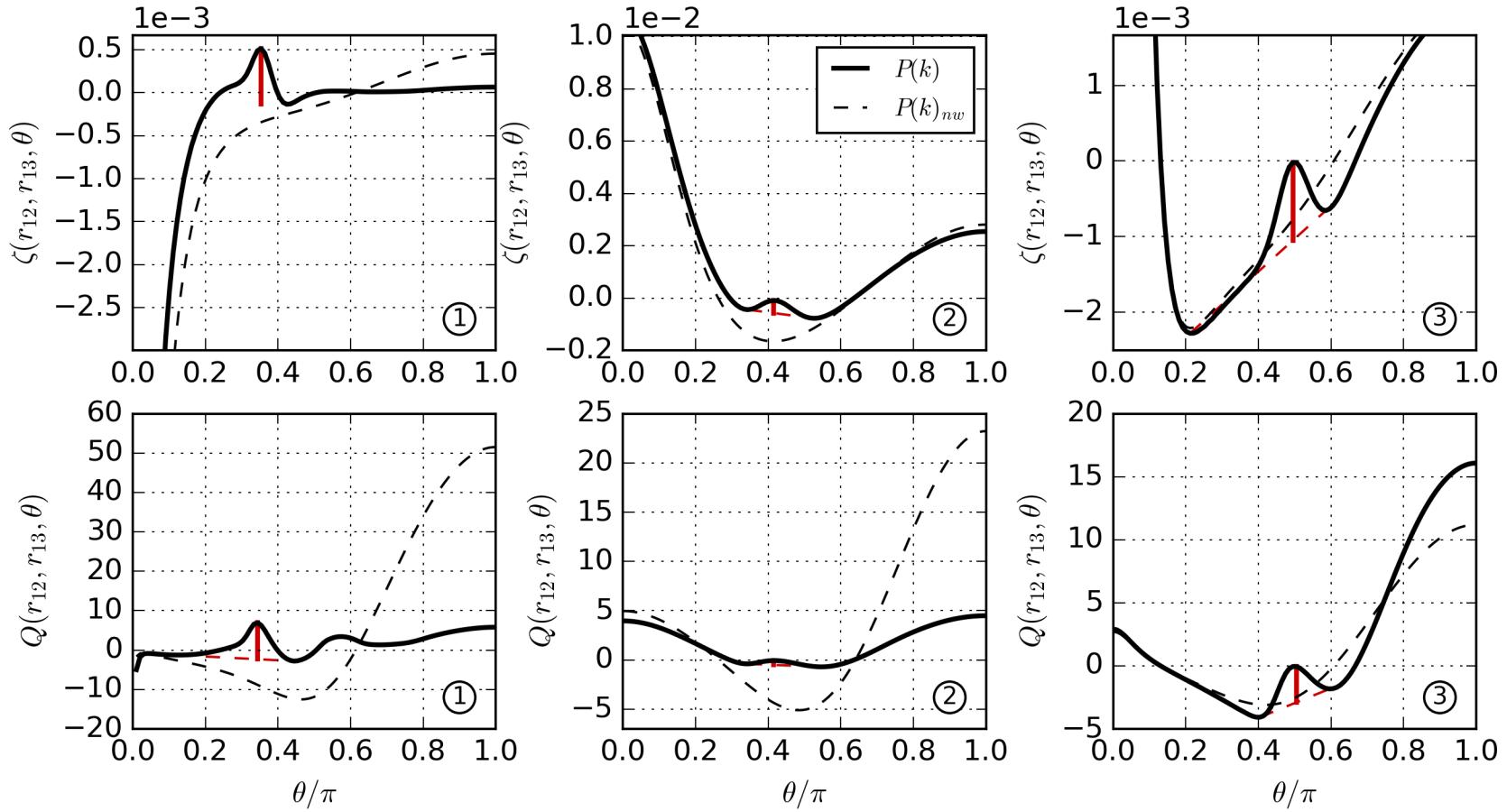
squeezing the BAO signal



scales	$\Delta\chi^2$
$r_{13} = [80-130] \text{ Mpc/h}$	90.5
$r_{13} = [60-140] \text{ Mpc/h}$	39.4
$r_{13} = [40-140] \text{ Mpc/h}$	3.9

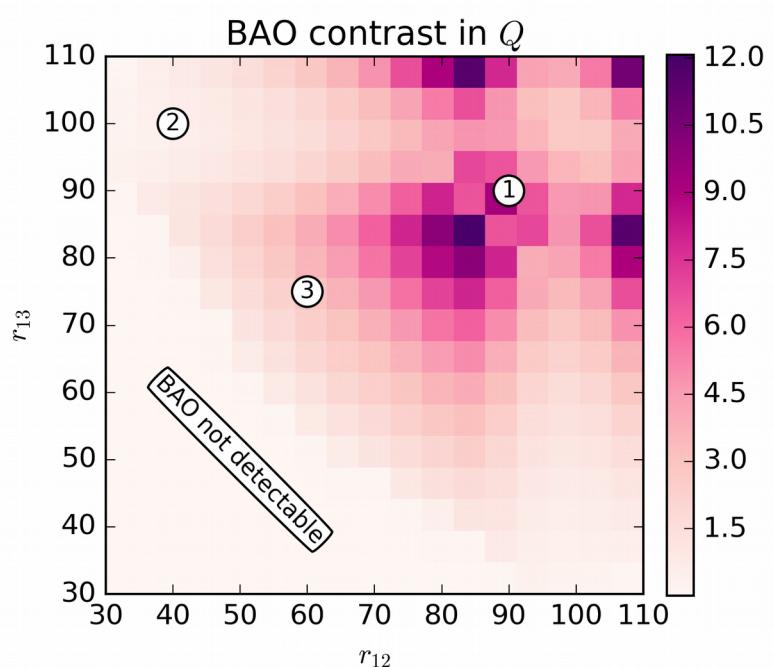
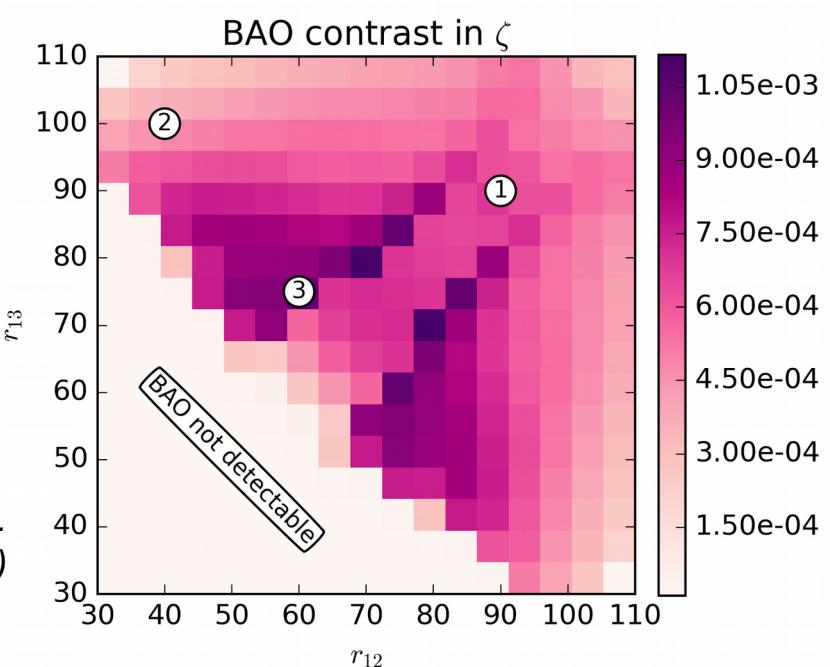
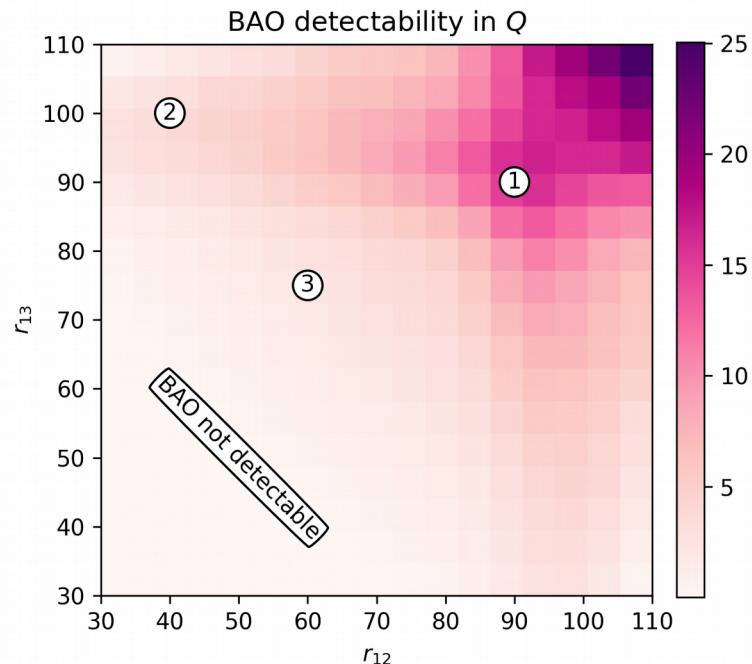
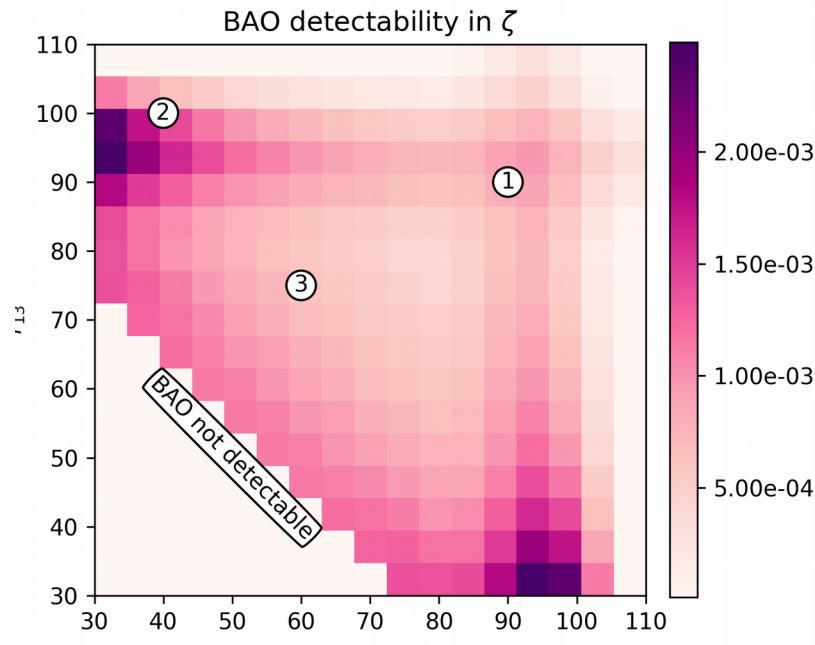
Moresco et al. (in prep)

# BAO detectability and SNR - definitions



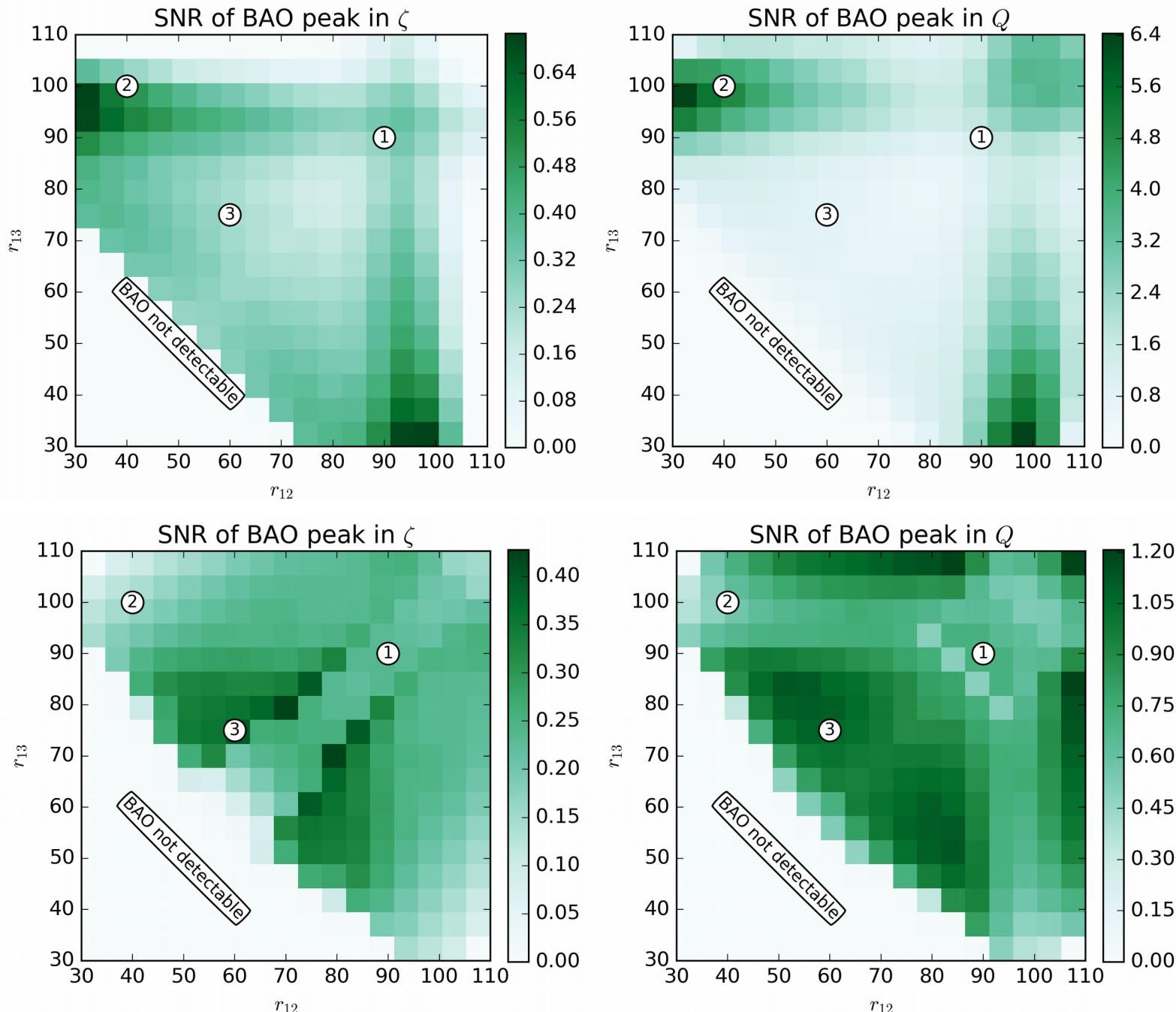
Moresco et al. (in prep)

# BAO detectability



Moresco et al.  
(in prep)

# BAO SNR



Moresco et al.  
(in prep)

# Conclusions

- 3PCF measured at different scales on the largest (to date) SDSS cluster catalog
- On large scales (below BAO) obtained a measurement of non-linear bias  
 $b_2 = 1.4 \pm 0.7$
- BAO may impact on 3PCF in different ways (squeezed/not squeezed, more peaked/flatter)
- significant detection of BAO signature in the 3PCF
- setup of a framework to identify the BAO signal in the 3PCF (both connected and reduced) with different approaches (BAO vs no BAO/BAO contrast)
- framework applicable to Euclid science case